

Finding the Sum of an Arithmetic Series (Explicit Notation)

1. Find the sum of the first 8 terms of the sequence $3 + 5 + 7 + 9 + \dots$

$$S_n = \frac{n(a_1 + a_n)}{2} \quad a_1 = 3$$

$$d = 2$$

$$S_8 = \frac{8(3 + 17)}{2} \quad n = 8$$

$$a_8 = 17$$

$$S_8 = 80$$

+2 +2 +2

$$a_n = a_1 + d(n-1)$$

$$a_1 = 3$$

$$d = 2$$

$$n = 8$$

$$a_8 = 3 + 2(8-1)$$

$$a_8 = 17$$

2. Find the sum of the first 20 terms of the sequence $4 + 7 + 10 + 13 + \dots$

$$S_n = \frac{n(a_1 + a_n)}{2} \quad a_1 = 4$$

$$d = 3$$

$$n = 20$$

$$a_n = 61$$

$$S_{20} = \frac{20(4 + 61)}{2}$$

$$S_{20} = 650$$

+3 +3 +3

$$a_n = a_1 + d(n-1) \quad a_1 = 4$$

$$a_{20} = 4 + 3(20-1) \quad d = 3$$

$$a_{20} = 61 \quad n = 20$$

3. Find the sum of the first 15 terms of the sequence $9 + 14 + 19 + 24 + \dots$

$$S_n = \frac{n(a_1 + a_n)}{2} \quad a_1 = 9$$

$$d = 5$$

$$n = 15$$

$$a_n = 79$$

$$S_{15} = \frac{15(9 + 79)}{2}$$

$$S_{15} = 660$$

+5 +5 +5

$$a_n = a_1 + d(n-1) \quad a_1 = 9$$

$$a_{15} = 9 + 5(15-1) \quad d = 5$$

$$n = 15$$

$$a_{15} = 79$$

4. Find the sum of the first 12 terms of the sequence $14 + 11 + 8 + 5 + \dots$

$$S_n = \frac{n(a_1 + a_n)}{2} \quad a_1 = 14$$

$$d = -3$$

$$n = 12$$

$$a_n = -19$$

$$S_{12} = \frac{12(14 + (-19))}{2}$$

$$S_{12} = -30$$

-3 -3 -3

$$a_n = a_1 + d(n-1) \quad a_1 = 14$$

$$a_{12} = 14 - 3(12-1) \quad d = -3$$

$$n = 12$$

$$a_{12} = -19$$

5. Find the sum of the first 67 terms of the sequence $2 + 11 + 20 + 29 + \dots$

$$S_n = \frac{n(a_1 + a_n)}{2} \quad a_1 = 2 \quad a_n = a_1 + d(n-1) \quad a_1 = 2$$

$$d = 9 \quad a_{67} = 2 + 9(67-1) \quad d = 9$$

$$n = 67 \quad a_{67} = 596 \quad n = 67$$

$$S_{67} = \frac{67(2 + 596)}{2}$$

$$S_{67} = 20033$$

6. Find the sum of the first 18 terms of the sequence $100 + 95 + 90 + 85 + \dots$

$$S_n = \frac{n(a_1 + a_n)}{2} \quad a_1 = 100 \quad a_n = a_1 + d(n-1) \quad a_1 = 100$$

$$d = -5 \quad a_{18} = 100 - 5(18-1) \quad d = -5$$

$$n = 18 \quad a_{18} = 15 \quad n = 18$$

$$S_{18} = \frac{18(100 + 15)}{2}$$

$$S_{18} = 1035$$

7. Find the sum of the first 10 terms of the sequence $-12 - 9 - 6 - 3 - \dots$

$$S_n = \frac{n(a_1 + a_n)}{2} \quad a_1 = -12 \quad a_n = a_1 + d(n-1) \quad a_1 = -12$$

$$d = 3 \quad a_{10} = -12 + 3(10-1) \quad d = 3$$

$$n = 10 \quad a_{10} = 15 \quad n = 10$$

$$S_{10} = \frac{10(-12 + 15)}{2}$$

$$S_{10} = 15$$

8. Find the sum of the first 25 terms of the sequence $6 + 2 - 2 - 6 - 10 - \dots$

$$S_n = \frac{n(a_1 + a_n)}{2} \quad a_1 = 6 \quad a_n = a_1 + d(n-1) \quad a_1 = 6$$

$$d = -4 \quad a_{25} = 6 - 4(25-1) \quad d = -4$$

$$n = 25 \quad a_{25} = -90 \quad n = 25$$

$$S_{25} = \frac{25(6 - 90)}{2}$$

$$S_{25} = -1050$$