

Start with the term after the one they give you
 a_{n-1} means the previous term

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Algebra II



Evaluating Recursive Sequences

1. Find a_4 of the sequence $a_n = 2a_{n-1} + 3$ where $a_1 = 1$.

$$\begin{aligned}a_2 &= 2(1) + 3 \\a_3 &= 2(5) + 3 \\a_4 &= 2(13) + 3\end{aligned}$$

$a_2 = 5$ $a_3 = 13$ $a_4 = 29$

2. Find a_5 of the sequence $a_n = 4a_{n-1} - 2$ where $a_2 = -3$.

$$\begin{aligned}a_3 &= 4(-3) - 2 \\a_4 &= 4(-14) - 2 \\a_5 &= 4(-58) - 2\end{aligned}$$

$a_3 = -14$ $a_4 = -58$ $a_5 = -234$

3. Find a_7 sequence

$$\begin{aligned}a_4 &= -2 \\a_n &= -3a_{n-1} + 4\end{aligned}$$
$$\begin{aligned}a_5 &= -3(-2) + 4 \\a_6 &= -3(10) + 4 \\a_7 &= -3(-26) + 4\end{aligned}$$

$a_5 = 10$ $a_6 = -26$ $a_7 = 82$

4. If $a_n = \frac{a_{n-1}}{2} + 2$ and $a_2 = 16$, find a_5

$$\begin{aligned}a_3 &= \frac{16}{2} + 2 \\a_4 &= \frac{10}{2} + 2 \\a_5 &= \frac{7}{2} + 2\end{aligned}$$

$a_3 = 10$ $a_4 = 7$ $a_5 = 5.5$

5. If $a_n = (a_{n-1})^2 - 4$ and $a_4 = 2$, find a_7

$$\begin{aligned}a_5 &= (2)^2 - 4 \\a_6 &= (0)^2 - 4 \\a_7 &= (-4)^2 - 4\end{aligned}$$

$a_5 = 0$ $a_6 = -4$ $a_7 = 12$

n is the term you're finding

6. Find the first four terms of the recursive sequence defined below.

$$a_1 = -3$$

$$a_n = a_{(n-1)} - n$$

$$\begin{aligned}a_2 &= -3 - 2 \\a_2 &= -5\end{aligned}$$

$$\begin{aligned}a_3 &= -5 - 3 \\a_3 &= -8\end{aligned}$$

$$\begin{aligned}a_4 &= -8 - 4 \\a_4 &= -12\end{aligned}$$

7. Find the 8th term for the sequence where $a_n = 5a_{n-1} + 2n$ where $a_5 = 3$

$$a_6 = 5(3) + 2(6)$$

$$a_6 = 27$$

$$a_7 = 5(27) + 2(7)$$

$$a_7 = 149$$

$$a_8 = 5(149) + 2(8)$$

$$\cancel{a_8 = 761}$$

8. A sequence is defined recursively by $a_1 = 16$ and $a_n = a_{n-1} - 4n$. Find a_4

$$a_2 = 16 - 4(2)$$

$$a_2 = 8$$

$$a_3 = 8 - 4(3)$$

$$a_3 = -4$$

$$a_4 = -4 - 4(4)$$

$$\textcircled{a_4 = -20}$$

9. The recursive formula to describe a sequence is shown below.

State the first four terms of this sequence. Can this sequence be represented using an explicit geometric formula? Justify your answer.

$$a_1 = 3$$

$$a_n = 1 + 2a_{n-1}$$

$$a_2 = 1 + 2(3)$$

$$a_2 = 7$$

$$a_3 = 1 + 2(7)$$

$$a_3 = 15$$

$$a_4 = 1 + 2(15)$$

$$a_4 = 31$$

No, there's addition

10. What is the fourth term of the sequence defined by $a_1 = 3xy^5$

1) $12x^3y^3$

2) $24x^2y^4$

3) $24x^4y^2$

4) $48x^5y$

$$a_2 = \left(\frac{2x}{y}\right)(3xy^5)$$

$$a_2 = 6x^2y^4$$

$$a_3 = \left(\frac{2x}{y}\right)(6x^2y^4)$$

$$a_3 = 12x^3y^3$$

$$a_n = \left(\frac{2x}{y}\right)a_{n-1}?$$

$$a_4 = \left(\frac{2x}{y}\right)(12x^3y^3)$$

$$a_4 = 24x^4y^2$$