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Geometry



## Transformations Review Sheet

1. If  $\triangle A'B'C'$  is the image of  $\triangle ABC$ , under which transformation will the triangles not be congruent?

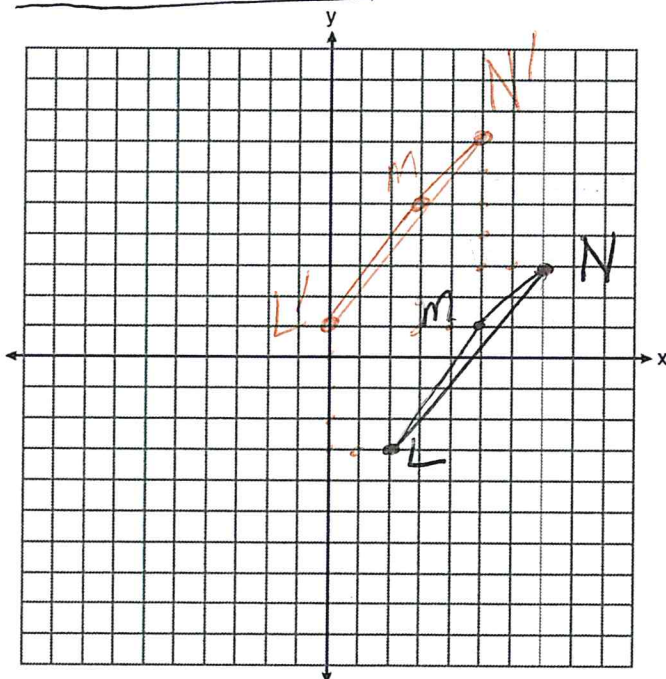
- 1) reflection over the x-axis  
2) translation to the left 5 and down 4  
3) dilation centered at the origin with scale factor 2  
4) rotation of  $270^\circ$  counterclockwise about the origin
- must be a dilation*

2. Under which transformation would  $\triangle A'B'C'$ , the image of  $\triangle ABC$ , not be congruent to  $\triangle ABC$ ?

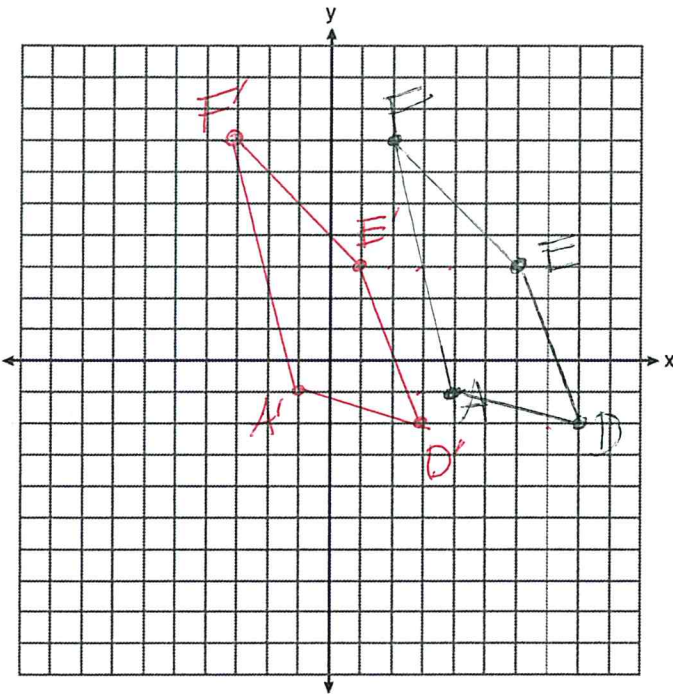
- 1) reflection through the point  $(2, -1)$   
2) rotation of  $90^\circ$  clockwise about the origin  
3) translation of 3 units right and 2 units down  
4) dilation with a scale factor of 2 centered at the origin
- must be a dilation*

3. What is the image of  $\triangle LMN$  with vertices  $L(2, -3)$ ,  $M(5, 1)$  and  $N(7, 3)$  after a translation 2 units to the left and 4 units up?

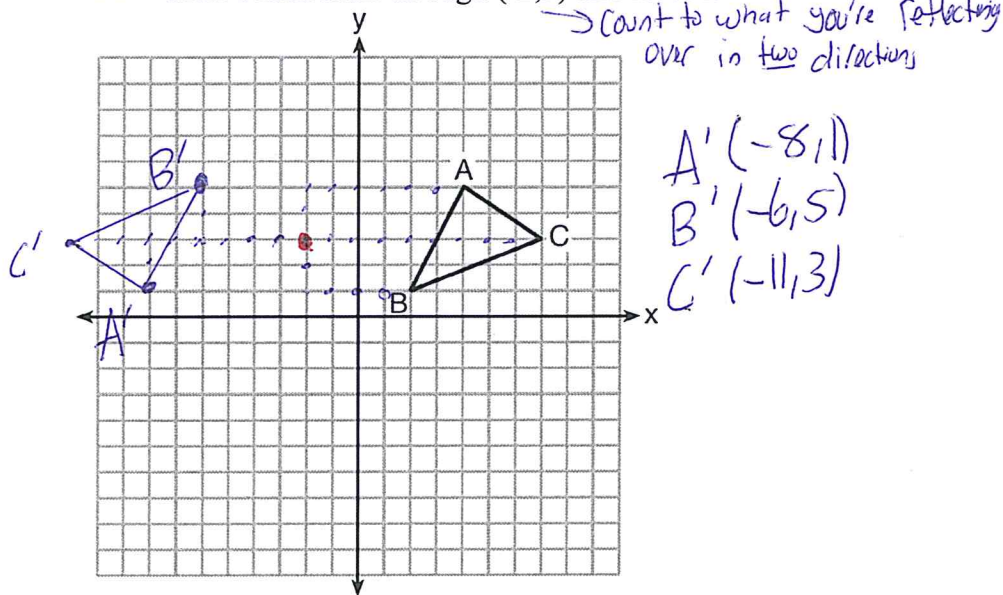
*can't*



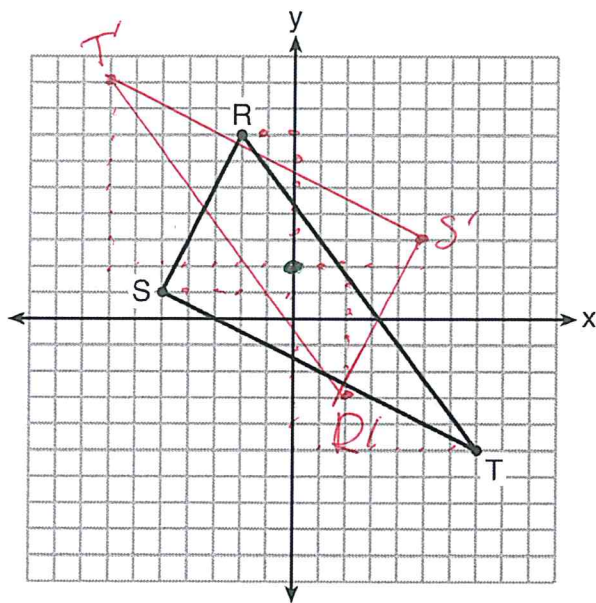
4. Graph the image of quadrilateral ADEF with vertices  $A(4, -1)$ ,  $D(8, -2)$ ,  $E(6, 3)$ , and  $F(2, 7)$  after a translation 5 units to the left?



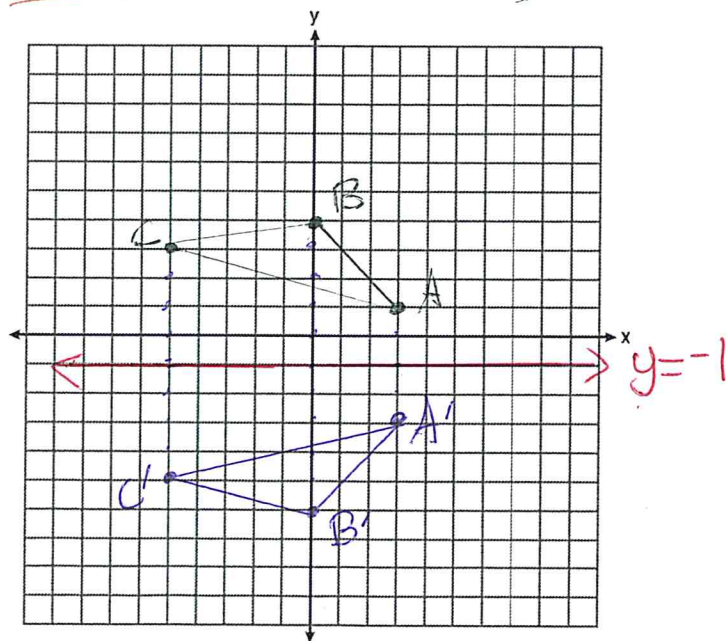
5. In the diagram below,  $\triangle ABC$  is graphed. Graph and state the coordinates of the image of  $\triangle ABC$  after a reflection through  $(-2, 3)$  and label it  $\triangle A'B'C'$ .



6. Triangle  $RST$  is graphed on the set of axes below. Graph the image of  $\triangle RST$  after a point reflection through  $(0,2)$  and label it  $\triangle R'S'T'$ .

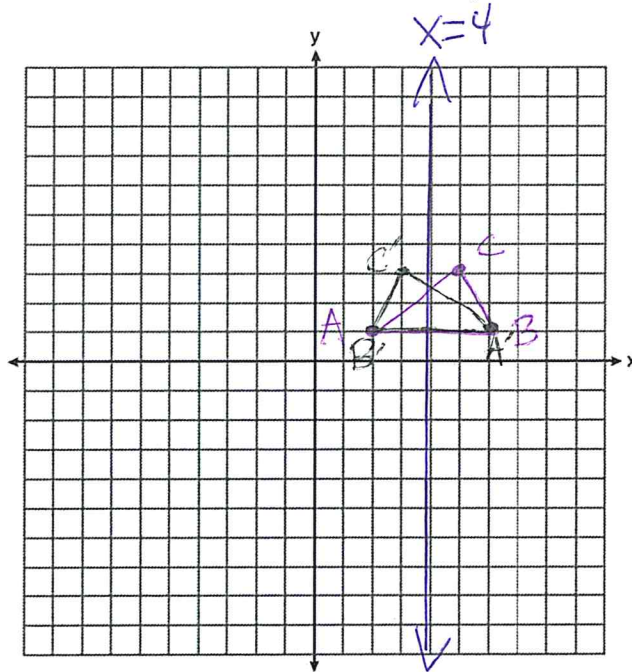


7. On the grid below, graph and label triangle  $ABC$  with vertices  $A(3,1)$ ,  $B(0,4)$ , and  $C(-5,3)$ . On the same grid, graph and label triangle  $A'B'C'$ , the image of  $ABC$  after a reflection over  $y = -1$ . Count to what you're reflecting over in one direction.





8. Triangle  $ABC$  has coordinates  $A(2, 1)$ ,  $B(6, 1)$ ,  $C(5, 3)$ . What is the image of this triangle after a reflection over the line  $x=4$ . Graph both the image and the pre image.



9. Triangle  $A'B'C'$  is the image of triangle  $ABC$  after a translation of 2 units to the right and 3 units up. Is triangle  $ABC$  congruent to triangle  $A'B'C'$ ? Explain why.

Yes! A translation is a rigid motion. A rigid motion preserves size and angle measure producing a congruent figure.

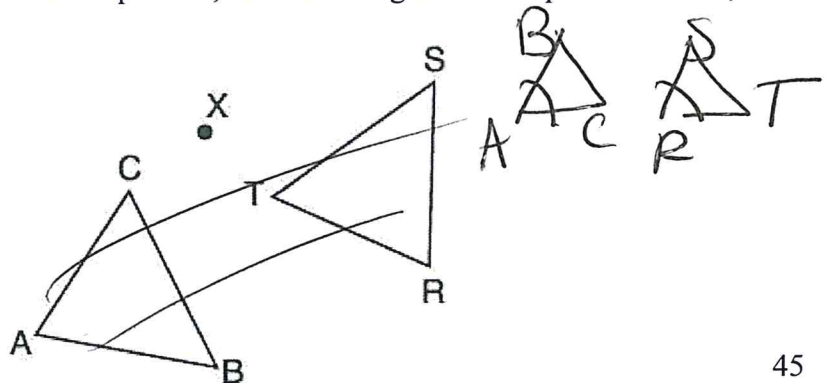
10. After a reflection over a line,  $\triangle A'B'C'$  is the image of  $\triangle ABC$ . Explain why triangle  $ABC$  is congruent to triangle  $\triangle A'B'C'$ .

A reflection is a rigid motion. A rigid motion preserves size and angle measure producing a congruent figure.

11. After a counterclockwise rotation about point  $X$ , scalene triangle  $ABC$  maps onto  $\triangle RST$ , as shown in the diagram below.

Which statement must be true?

- 1)  $\angle A \cong \angle R$   
 2)  $\angle A \cong \angle S$   
 3)  $\overline{CB} \cong \overline{TR}$   
 4)  $\overline{CA} \cong \overline{TS}$



12. In the diagram below, a sequence of rigid motions maps  $ABCD$  onto  $JKLM$ .

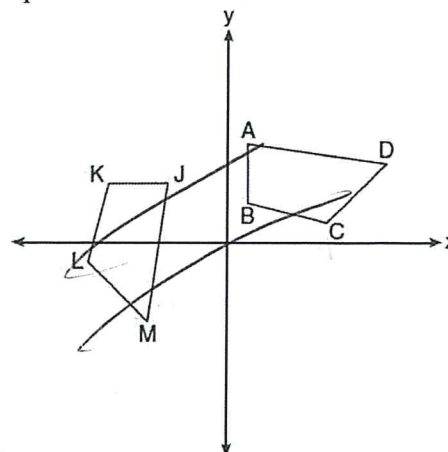
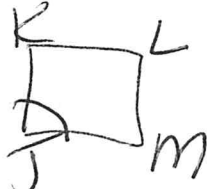
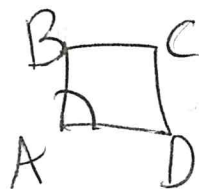
Which of the following statements must be true?

3)  $\angle L \cong \angle B$

3)  $\overline{JK} \cong \overline{AC}$

4)  $\angle A \cong \angle J$

4)  $\overline{JM} \cong \overline{AB}$



13. Which of the following sequences of rigid motions would map  $\triangle GIA$  onto  $\triangle JET$ ?

1) point reflection through  $(0.5, 0.5)$  followed by a translation

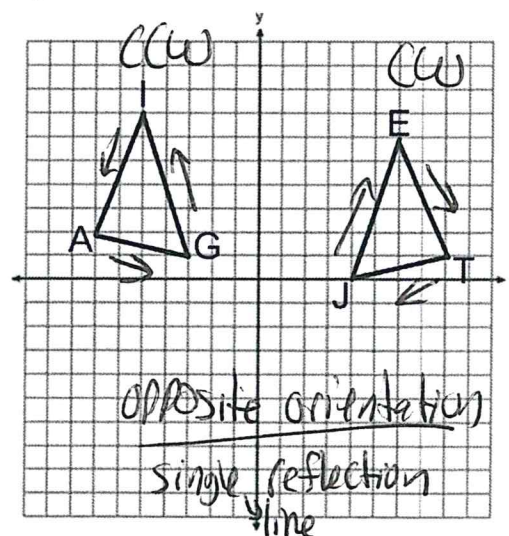
11 right and 1 down

2) reflection over the y-axis followed by a translation right 1 and down 1

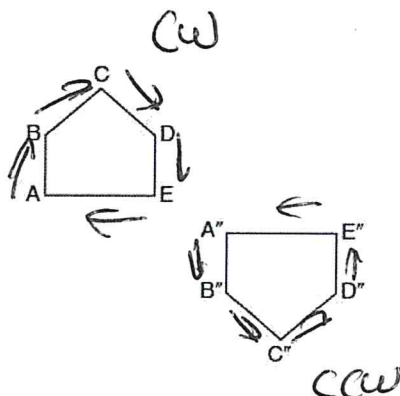
3) rotation of 90 degrees clockwise centered at the origin followed by a translation right 1 and up 1

4) reflection over  $x=1$  followed by a reflection over the x-axis

double reflection



14. Identify which sequence of transformations could map pentagon  $ABCDE$  onto pentagon  $A''B''C''D''E''$ , as shown below.



opposite orientation

must be a

single line reflection

1) dilation followed by a rotation

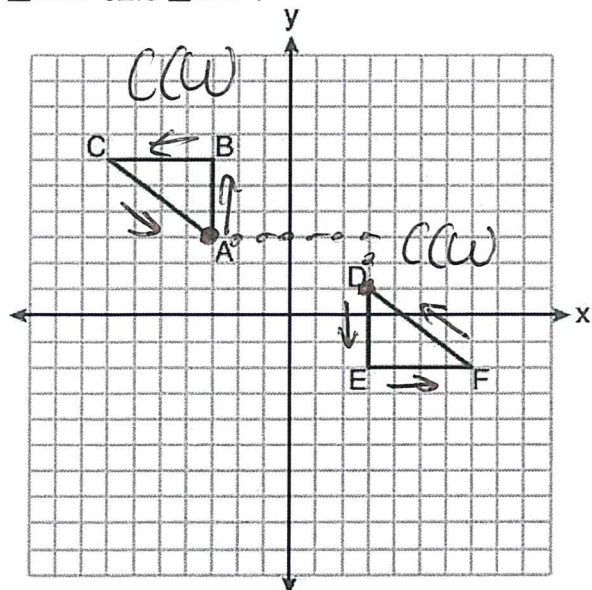
2) translation followed by a rotation

3) line reflection followed by a translation

4) line reflection followed by a line reflection

double reflection

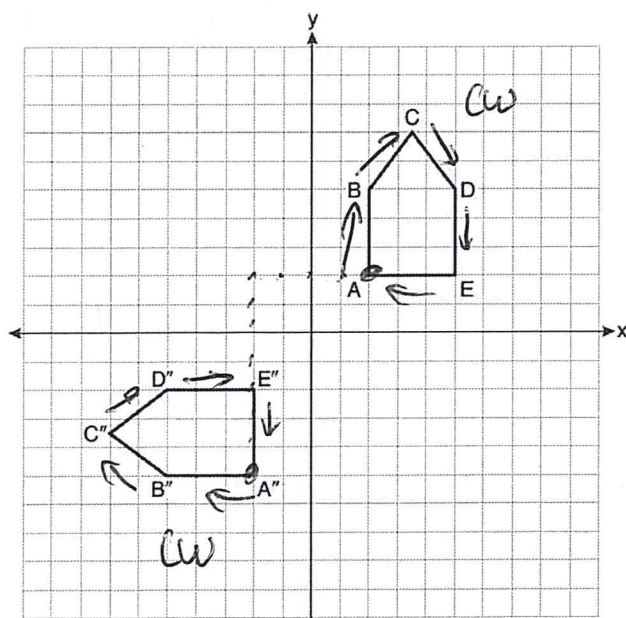
15. On the set of axes below,  $\triangle ABC \cong \triangle DEF$ . Describe a sequence of rigid motions that maps  $\triangle ABC$  onto  $\triangle DEF$ .



Same orientation  
rotation

rotate  $\triangle ABC$   $180^\circ$  clockwise centered at A  
followed by a translation 6 units right and  
2 units down.

16. On the set of axes below, pentagon  $ABCDE$  is congruent to  $A''B''C''D''E''$ . Describe a sequence of rigid motions that maps pentagon  $ABCDE$  onto  $A''B''C''D''E''$ .

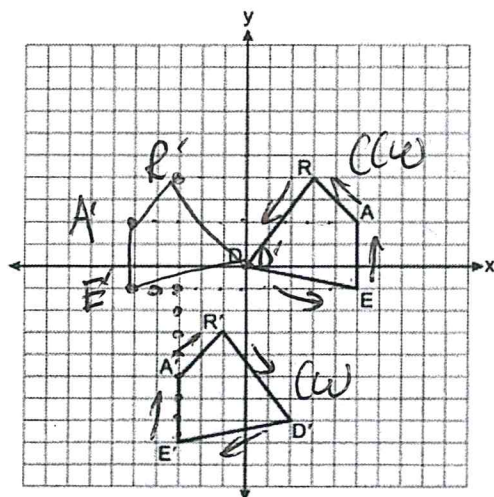


rotate  $ABCDE$   $90^\circ$  counter-clockwise  
centered at A followed by a translation  
4 left and 7 down.

Same orientation  
rotation



17. Quadrilateral  $DEAR$  and its image, quadrilateral  $D'E'A'R'$ , are graphed on the set of axes below. Describe a sequence of transformations that maps quadrilateral  $DEAR$  onto quadrilateral  $D'E'A'R'$ .

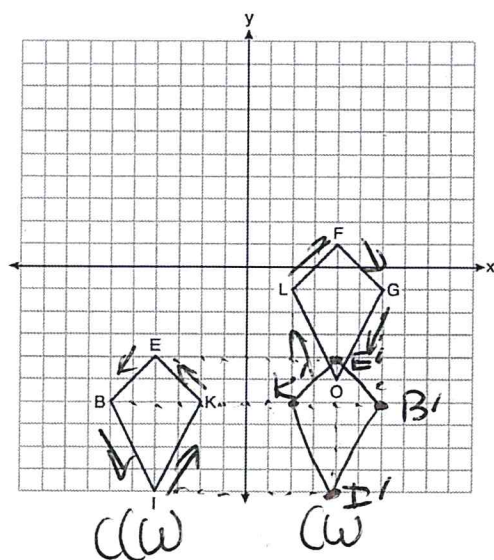


opposite orientation

reflection

Reflect  $DEAR$  over the  $y$ -axis followed by a translation 2 right and 7 down.

18. Quadrilaterals  $BIKE$  and  $GOLF$  are graphed on the set of axes below. Describe a sequence of transformations that maps quadrilateral  $BIKE$  onto quadrilateral  $GOLF$ .



opposite orientation

reflection

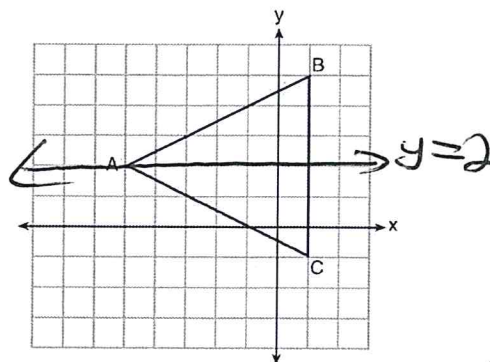
Reflect  $BIKE$  over the  $y$ -axis followed by a translation 5 units up.

line of reflection = line of symmetry  
center of rotation = center of shape

19. Triangle  $ABC$  is graphed on the set of axes below.

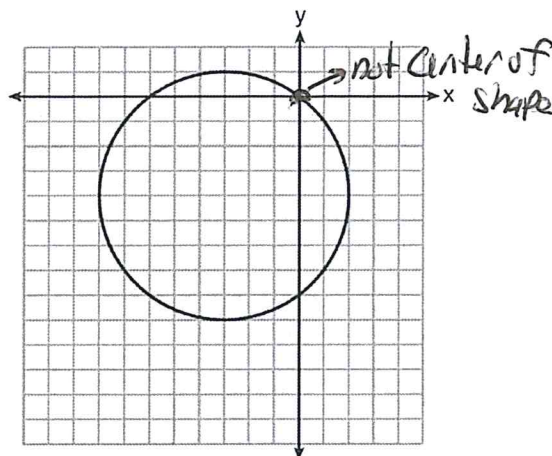
Which transformation maps  $\triangle ABC$  onto itself?

- 1) Reflection over the  $x$ -axis
- 2) Reflection over  $x = 2$
- 3) Reflection over  $y = 2$
- 4) Reflection over  $x = -2$



20. Which transformation does not map the circle in the diagram below onto itself?

- 1) Rotation of 90 centered at the origin
- 2) Reflection over the line  $x = -3$
- 3) Rotation of 90 centered at  $(-3, -4)$
- 4) Reflection over the line  $y = -4$



21. A regular octagon is rotated  $n$  degrees about its center, carrying the octagon onto itself. The value of  $n$  could be

- 1)  $10^\circ$
- 2)  $150^\circ$

② 225°  $45(5)$   
4) 252°

$\frac{360}{8} = 45$

22. Which of the following rotations would not map a regular pentagon onto itself?

- (1) 144°  $72(2)$
- (2) 120°
- (3) 216°  $72(3)$
- (4) 720°  $72(10)$

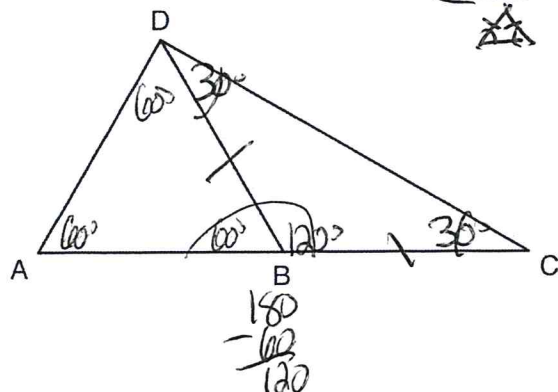
$\frac{360}{5} = 72$

### Spiral Review

#### Complex Triangle Problems:

- 1) The three angles of a triangle add to equal  $180^\circ$ . Look for triangles.
- 2) Linear pairs add to  $180^\circ$ . Look for linear pairs.
- 3) Isosceles triangle has congruent angles opposite congruent sides (given congruent sides).
- 4) Equilateral triangle has angles 60, 60, 60 (given equilateral triangle).
- 5) An angle bisector cuts an angle into two congruent halves (given bisected angles).
- 6) Use parallel lines cut by a transversal (extend and follow the transversal, fill in 8 angles.)

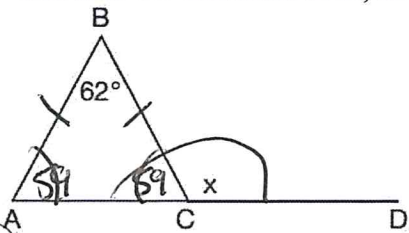
23. In the diagram below of  $\triangle ACD$ ,  $B$  is a point on  $\overline{AC}$  such that  $\triangle ADB$  is an equilateral triangle, and  $\triangle DBC$  is an isosceles triangle with  $\overline{DB} \cong \overline{BC}$ . Find  $m\angle C$ .



$\frac{180}{2} = 90$   
 $\frac{60}{2} = 30$



24. Given  $\triangle ABC$  with  $m\angle B = 62^\circ$  and side  $\overline{AC}$  extended to  $D$ , as shown below.



$$\begin{array}{r} 180 \\ - 62 \\ \hline 118 \end{array}$$

$$\frac{118}{2} = 59$$

Which value of  $x$  makes  $\overline{AB} \cong \overline{CB}$ ?

- 1)  $59^\circ$
- 2)  $62^\circ$

3)  $118^\circ$

4)  $121^\circ$

$$\begin{array}{r} 180 \\ - 59 \\ \hline 121 \end{array}$$

